A Three-Dimensional X-ray Redetermination of the Crystal Structure of Ammonium Perchlorate

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The crystal structure of ammonium perchlorate has been redetermined by X-ray three-dimensional analysis of 800 reflexions collected with Mo K α monochromatized radiation on an automatic fourcircle diffractometer. The cell parameters, redetermined with the same apparatus are: a=9.227, b=7.454, c=5.819 Å (24°C), Z=4, space group $Pna2_1$ (C_{2v}^2) from systematic absences and by successful refinement. The previous space group, Pnma, used for the two-dimensional analysis, did not allow a three-dimensional refinement. The positional and anisotropic thermal parameters of the non-hydrogen atoms were refined by the least-squares method. An almost spherical distribution of the hydrogen atoms around the nitrogen atom was introduced into the calculation. Final R=0.050. Residual electron density maxima were observed from difference Fourier syntheses around the nitrogen atom at distances of 0.8-0.9 Å. They make tetrahedral angles to nitrogen and have short $H \cdots O$ distances (2.15-2.50 Å) from eight neighbouring oxygen atoms, indicating that the ammonium ion does not have a completely free rotation.

Introduction

Thé crystal structure of ammonium perchlorate has been assigned to the orthorhombic space group Pnma and studied by X-ray Fourier projections (90 h0l reflexions with R = 0.136 and 35 hk0 reflexions with R=0.128) by Venkatesan (1957), who suggested an ordered hydrogen-bonded arrangement of the ammonium ion, and from room-temperature single-crystal neutron diffraction by two-dimensional syntheses (120 h0l and 44 hk0 reflexions with weighted R = 0.08) by Smith & Levy (1962) who concluded that the orientation of the ammonium ion is a highly disordered one, the ion undergoing a free or nearly free rotation. A rotating ion is also supported by the infrared spectrum (Waddington, 1958), by heat capacity studies between 5 and 350 K (Justice & Westrum, 1961), by cold neutron studies (Rush, Taylor & Havens, 1961) and by n.m.r. studies (Ibers, 1960; Richards & Shaefer, 1961) at low temperatures. Since only two-dimensional X-ray or neutron diffraction data have been used until now for the crystal structure determination of ammonium perchlorate, we have undertaken the redetermination of this structure by three-dimensional X-ray counter data.

Experimental

An elongated prismatic crystal $(0.35 \times 0.40 \times 0.5 \text{ mm})$ was used for all the measurements. The orientation of the crystal, mounted along the elongated axis, and the analyses of the systematic absences were carried out with Weissenberg and precession photographs. The lattice parameters were determined and the intensities of the reflexions were recorded with Mo K α monochromatized radiation ($\lambda = 0.71069$ Å) on a Philips PW1100 automatic four-circle diffractometer connected on-line with a computer. The centring of the crystal and the determination of the lattice parameters were automatically performed by means of about 25 strongest reflexions randomly chosen by the diffractometer in a wide region of reciprocal space.

On the basis of the systematic absences two different space groups may be chosen, implying a different orientation of the crystallographic axes: the centrosymmetric space group *Pnma* (D_{2h}^{16}) used by Smith & Levy (1962), by Venkatesan (1957) and by other previous authors (see references therein), and the noncentrosymmetric space group *Pna2*₁ (C_{2r}^9), by permutation of the *b* and *c* axes of the previous orientation.

Independently of the positional parameters given by the authors cited above, we solved the structure by direct methods using the LSAM program (Germain, Main & Woolfson, 1971) in the space group *Pnma*. By using 168 reflexions all the non-hydrogen atoms were located and well defined with three-dimensional Fourier syntheses. Furthermore it was impossible to refine the structure in this space group by least-squares methods using all the three-dimensional data, either with the Smith & Levy (1962) parameters or with the new ones, because the reliability index R, with an initial value of about 0.27, was unrefinable and divergent.

By using 55 *hk*0 reflexions in the *Pnma* group orientation the structure was refinable with isotropic temperature factors for non-hydrogen atoms to a reliability index R=0.07 and x, y positional parameters very close to the values given by Smith & Levy (1962). It was therefore evident that the centrosymmetric space group *Pnma* is incorrect. The refinement was then performed in the space group $Pna2_1$ and converged very rapidly to reliable values of the index R, the anisotropic parameters and the interatomic distances and angles.

Crystal data

Ammonium perchlorate, NH₄ClO₄. Orthorhombic pyramidal; space group $Pna2_1$ (C_{2v}^9 , No. 33) from systematic absences (0kl, k+l=2n+1; h0l, h=2n+1) and by successful refinement. $a=9\cdot227$, $b=7\cdot454$, c= $5\cdot819$ Å, at 24°C. $V=400\cdot2$ Å³, F.W. 145.50, Z=4, F(000)=296. $D_c=2\cdot415$ g cm⁻¹. In this orientation the crystals are elongated along the *b* axis.

The X-ray intensities were corrected for Lorentz and polarization factors; only the values of $F_o > 1.5\sigma(F_o)$ were used for the calculations. From a Wilson plot of the data overall scale and temperature factors were obtained. The positional parameters, the isotropic and anisotropic thermal parameters of the nonhydrogen atoms and the scale factors (K) for each hkl layer were then refined by the least-squares method using the program *MIQUAD* of Immirzi (1967a) until convergence of the R value at 0.055. The atomic scattering factors given by Hanson, Herman, Lea & Skillmann (1964) were used.

102 fractional (0.039 H) hydrogen atoms (hydrogenoids) were then introduced into the calculation with the isotropic temperature factor (B=4.30) of the nitrogen atom and located in equidistant and symmetrical positions around the nitrogen atom on a sphere



Fig. 1. Orthographic projection of the unit cell on the xy plane. ORTEP plot of thermal ellipsoids scaled to include 50% probability. of radius 1.03 Å, at a distance of about 0.35 Å from each other. With this distribution the hydrogenoids are regularly interpenetrated, giving an almost spherical electron distribution. The weights of the reflexions were calculated with the formula $1/w = \sigma^2 + 0.004 F_o^2$ (Gilmore & Woodward, 1971).

The positional and thermal parameters of the nonhydrogen atoms were refined until the reliability index converged to a final R value = 0.050, the fitting to 1.02and the variation of the positional and anisotropic temperature factors of the non-hydrogen atoms were of the same order as their standard deviations. Two different distributions of hydrogen atoms gave identical values of R and of interatomic distances and angles. The final positional and thermal parameters of the non-hydrogen atoms are given in Table 1, the observed and calculated structure factors in Table 2 and the interatomic distances and angles in Table 3. An orthographic xy projection of the unit cell (Fig. 1) and an xz projection of the perchlorate ion thermal ellipsoids (Fig. 2) were plotted with the ORTEP program of Johnson (1965).

Three-dimensional difference Fourier syntheses, using structure factors not including the contribution of the hydrogen atoms, were calculated with the FOUR 3D program of Immirzi (1967b) in the regions occupied by the perchlorate and the ammonium ions. Residual electron density maxima were observed around the nitrogen atom (Fig. 3, Table 4). Four of these correspond to a fixed position of the ammonium ion. By using the hydrogen atoms in these fixed positions for the refinement, the same convergent reliability index R=0.050 was obtained, with a fitting of 1.07. The interatomic distances and angles are given in square brackets in Table 3.

Results and discussion

The assignment of ammonium perchlorate to the centrosymmetric space group *Pnma* seems to have been based on the fact that from morphological studies the crystal was considered to belong to the orthorhombic bipyramidal class (Venkatesan, 1957). Consequently chlorine, nitrogen and two oxygen atoms were located, in the *Pnma* group, in a special position with $y = \pm 0.250$, the other two oxygen atoms being specularly symmetrical with respect to a symmetry plane normal to the y axis at y=0.250.

Table 1. Fractional coordinates and thermal parameters

Coordinates are $\times 10^5$. Thermal parameters are defined by	
$T = \exp\left[-\frac{1}{4}(\hat{B}_{11}a^{*2}h^{2} + B_{22}b^{*2}k^{2} + B_{33}c^{*2}l^{2} + 2B_{12}a^{*5}hk + 2B_{13}a^{*}c^{*h}l + 2B_{23}b^{*}c^{*k}l\right]$	$) \times 10^{-3}].$

	x	У	z	B ₁₁	B ₂₂	B ₃₃	<i>B</i> ₁₂	B ₁₃	B ₂₃
Cl	43199 (5)	30821 (6)	25082 (33)	2090 (15)	7247 (15)	2115 (16)	-110 (11)	92 (46)	211 (34)
O(1)	42064 (31)	19487 (36)	45055 (45)	4632 (134)	9190 (108)	1678 (79)	389 (79)	-178(72)	487 (66)
O(2)	42004 (26)	19770 (31)	4628 (55)	3207 (88)	8271 (88)	3525 (115)	132 (58)	- 40 (74)	- 905 (77)
O(3)	56815 (20)	39857 (41)	25745 (93)	3359 (78)	10618 (114)	5627 (142)	- 1990 (73)	656 (158)	-790 (278)
O(4)	31487 (23)	43483 (26)	24550 (63)	4179 (77)	7993 (64)	4136 (92)	1116 (58)	-1223 (145)	-42 (137)
Ν	18094 (22)	33411 (25)	-24876 (87)	2505 (66)	7819 (67)	3109 (83)	116 (51)	-1108 (164)	56 (173)

Table 2. Observed and calculated structure factors $(\times 10)$

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The new x, y, z coordinates found in this work by using the non-centrosymmetric space group Pna2, may be transformed into the x', y', z' coordinates corresponding to those found by Venkatesan (1957) and Smith & Levy (1962) using the equivalences: $x'=x, y'=z, z'=\frac{1}{2}-y$. These new parameters differ from those found by Smith & Levy (1962) by an average value of ± 0.003 , a little greater than the standard deviations given by these authors (0.001-0.002). Also the deviations of the new y' values from ± 0.250 are very small (Cl +0.001, O(3) -0.004, O(4) + 0.007, N + 0.001) and the difference 0.500 y'[O(2)] - y'[O(3)] = 0.003. It is likely that such small deviations from the conditions of centrosymmetry do not sensibly affect the morphology of the crystal and the description of the structure as centrosymmetric by using few reflexions either in the case of two-dimensional analysis (Venkatesan, 1957; Smith & Levy, 1962), or in the case of direct method determination with 168 three-dimensional strong reflexions (present work). For reasons of symmetry the structure is refinable on hk0 and h0l projection in the Pnma space group.

The Cl-O distances (Table 3) show differences which in part may be due to the imperfect localization of the hydrogen atoms, because of their statistical disorder, but as the $N \cdots O$ distances indicate hydrogen interactions between ammonium and perchlorate ions, it is



Fig. 2. Perchlorate ion projection on the xz plane. ORTEP plot of thermal ellipsoids scaled to include 50% probability.



Fig. 3. Residual electron densities around the nitrogen atom: (right) in the xz section through the centre of the nitrogen atom; (left) composite drawing with sections through the centre of the hypothetical fractional hydrogen atoms (Table 4). Dotted lines at $0.8 \text{ e} \text{ Å}^{-3}$; line intervals of $0.05 \text{ e} \text{ Å}^{-3}$.

Table 3. Interatomic distances (Å) and angles (°) and their e.s.d.'s

In square brackets are given the bond distances and angles obtained with a fixed position of the ammonium ions.

Bond distances								
Cl-O(1)	1.441 (3) [1.4	44 (3)]	Cl-O(3)	1.426 (2) [1.424 (2)]			
Cl-O(2)	1.452 (3) [1.4	41 (4)]	Cl-O(4)	1.435 (2) [1.435 (2)]			
	Cl-O Average 1.438 [1.436]							
Other distances								
	N-O(2) [4]	2.97	N-O(2) [3]	3.10				
	N-O(2) [1]	2.98	N-O(4) [1]	3.22				
	N-O(4) [6]	2.98	N-O(4) [2]	3.28				
	N-O(1) [5]	2.98	N-O(3) [5]	3.51				
	N-O(1) [2]	3.01	N-O(3) [4]	3-57				
	N=O(1)[3]	3.08	N-O(3) [6]	3.98				
Bond angles								
O(1) - Cl - O(2)	108.8 (1) [108	3·7 (1)]	O(2)-Cl-O	(3) 110.9	(1) [110.6 (1)]			
O(1) - C1 - O(3)	108.6 (1) [108	3·7 (1)]	O(2)-Cl-O	(4) 107.4	(1) [107.4 (1)]			
O(1)ClO(4)	110.4 (1) [110)·4 (1)]	O(3)-Cl-O	(4) 110.7	' (1) [111·1 (1)]			
	0-C	l-O Average 1	09.5 [109.5]					
Other angles								
O(2) [3]-N-O(3) [4]	130.8	O(4) [2]-N-	-O(1) [3]	104.7			
O(1) [3]-N-O(3) [5]	130.5	O(2) [1]-N	-O(2) [4]	103.9			
O(4) [1]-N-O(4) [2]	127.1	O(4) [1]-N-	–O(4) [6]	103.8			
O(1) [2]-N-O(3) [4]	121.8	O(1) [2]-N	-O(1) [5]	103.1			
O(2) [1]-N-O(3) [5]	121.5	O(4) [2]-N	-O(4) [6]	102.4			
O(3) [4	J-N-O(3) [5]	110.4	O(1)[5]-N	-O(3) [4]	102.4			
O(1) [2] O(2) [1]	J-N-O(4) [1]	108.6	O(2) [4]-N	-0(3)[5]	101.2			
O(2) [1]	J-N-O(4) [2]	108.5	O(2) [3]-N	-O(2) [4]	92.8			
O(2) [1]	J = N = O(1) [3] J = N = O(2) [3]	107.9	O(1)[5]=N	-O(2) [3]	91.6			
O(1) [2 O(4) [1	I = N = O(2) [3]	104.8	$O(3) [4] - N_{1}$	-O(1) [3]	91.4			
Asymmetric units								
[1]	x y	z	[4] x -	$-\frac{1}{2}$ $\frac{1}{2}-y$	Z			
[2]	x y	z-1	[5] x -	$-\frac{1}{2}$ $\frac{1}{2}-y$	z - 1			
[3]	$\frac{1}{2}-x$ $\frac{1}{2}+y$	$z - \frac{1}{2}$	[0] 2 -	$-x y - \frac{1}{2}$	$z-\frac{1}{2}$			

Table 4. Residual electron density maxima around the nitrogen atom located in a tetrahedral configuration, corresponding to hypothetical fractional hydrogen atoms: fractional coordinates (×10³), N-H distances (Å), H-N-H angles (°) and H···O distances (Å)

	x	У	z	e Å⁻³	N–H
H(1)	150	220	- 245	0.8	0.90
H(2)	273	350	-250	1.0	0.86
H(3)	150	375	-125	0.9	0.83
H(4)	146	375	- 378	0.9	0.87
H(1)-N-	H(2)	116.5	H(2	-N-H(3)	107-2
H(1)–N–	H(3)	102.5	H(2	()-N-H(4)	108.1
H(1)-N-	H(4)	103.6	H(3)-N-H(4)	119.4
$H(1)\cdots 0$	D(4) [6]	2.15	H(3)···O(1)	3] 2.51
$H(1) \cdots 0$	D(2)[4]	2.78	H	$3) \cdots O(2)$	4 2.41
$H(1) \cdots 0$	D(1)[5]	2.83	H	3)···O(4)	1] 2.68
$H(2) \cdots ($	D(1) [2]	2.50	H	$(4) \cdots O(1)$	[5] 2 ·36
$H(2)\cdots 0$	D(2) [1]	2·4 7	H(4)···O(2)	[3] 2.52

likely that the Cl–O distance is also influenced by the strength of the O···HN bonds. The multiplicity of the O···N short contacts (Table 3) confirms a statistically dynamic orientation of the ammonium ion around the nitrogen atomic position. However, many O···N···O angles (Table 3) near to the tetrahedral value seem to indicate that some positions of the ammonium ion could be more favoured.

The three-dimensional difference Fourier syntheses show residual positive electron densities of 0.4–0.5 e Å⁻³ in the positions occupied by chlorine and oxygen atoms and of 0.6–0.7 e Å⁻³ in the positions of their close neighbours. Definite maxima of greater electron densities (0.8–1.0 e Å⁻³) are observed around the nitrogen atom at a distance of about 0.8–0.9 Å, that is in the region occupied by the cloud of hydrogen atoms. Fig. 3 shows (right) the maxima appearing in the xz section through the y position of nitrogen atom, and (left) four maxima located in an almost tetrahedral position around the nitrogen atom.

As shown by the N-H distances and angles (Table 4), they may reasonably be interpreted as fractional hydrogen atoms corresponding to a favoured orientation of the ammonium ion. All these 'hydrogenoids' have at least two short $H \cdots O$ distances from neighbouring oxygen atoms. All these $H \cdots O$ distances are almost equivalent and seem to indicate that this favoured position corresponds to a rather equilibrated orientation of the ammonium ion with each hydrogen located 'between' two oxygen atoms. These contacts involve all the eight oxygen atoms with the shortest $O \cdots N$ distances (Table 3).

The presence of other maxima and the elongated form of the maximum 'H(2)', which may be due to a superposition of several 'hydrogenoids' could indicate

that other favoured orientations of the ammonium ion may be present in this structure. In any case it seems reasonable to conclude that the rotation of the ammonium ion is not completely free, the distribution of oxygen atoms around the nitrogen atom imposing a certain number of preferential orientations, as that described above.

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The Crystal Structure of trans-1-Amino-1,3-dicarboxycyclopentane

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trans-1-Amino-1,3-dicarboxycyclopentane crystallizes with acetic acid of crystallization in the space group $Pca2_1$, with Z=4, $a=9\cdot122$ (5), $b=13\cdot964$ (9), $c=8\cdot667$ (5) Å, V=1104 (1) Å³. $D_x=1\cdot40$ and $D_m=1\cdot39$ g cm⁻³. Diffractometer data, collected with monochromatic Cu Ka radiation, consisted of 1104 independent reflections of which 190 were less than $2\cdot33\sigma(I)$. The structure was solved by direct methods and refined by a full-matrix least-squares procedure to the final residual $R=0\cdot065$. All hydrogen atoms were located and were refined isotropically. There is an intramolecular hydrogen bond between the 1-amino group and the 3-carboxyl group and the crystal packing is dominated by hydrogen-bond formation. The conformation of the cyclopentane ring is intermediate between that of an envelope and of a half-chair.

Introduction

It has been shown that 1-amino-1,3-dicarboxycyclopentane, an analogue of glutamate, is a substrate for glutamine synthetase (Stephani, Rowe, Gass & Meister, 1972). The enzyme interacts with one isomer of the racemic *cis* form of the analogue, but not with the *trans* form. A crystallographic study of the *trans* analogue has been undertaken as part of a study of the conformations of both isomers.

Experimental

A mixture of the *cis* and *trans* isomers was separated by the procedure of Stephani, Rowe, Gass & Meister (1972). The crystal data are given in Table 1. Since the crystals, which grew as colorless needles in glacial acetic acid, formed in a noncentrosymmetric space group, it appears that the racemic mixture was resolved into its optical isomers on crystallization. Threedimensional data were collected on a Syntex automated diffractometer equipped with a graphite monochromator and Cu K α radiation using the θ -2 θ scan tech-

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